24 people were asked to rank the following sports in order of most favorite to least favorite. A - Basketball; B - Baseball; C - Football; D - Soccer. The following linear graphs illustrates the results along with the number of people in favor.
$\mathrm{A}-\mathrm{A}$
$\mathrm{B}-\mathrm{Z}$
$\mathrm{C}-\mathrm{Z}$
$\mathrm{D}-\mathrm{Z}$
9
B
A
D
C

| C |
| :--- |
| $\mathrm{C}-\mathrm{A}$ |
| $\mathrm{A}-1$ |
| $\mathrm{~B}-\mathrm{Z}$ |



Plurality Method: Who has the most first place votes? A (9)
Majority Method: The winner must have half plus one of the votes. No majority. Need $12+1$ votes.

## Run off Method:

- Choose the two candidates that have the most first-place votes.
- Eliminate other choices.
- See who has the higher rankings now.
- Is there a majority? $(24 / 2)+1=13$ is needed for a majority. No majority $\rightarrow$ runoff
$\mathrm{A}-\mathrm{A}$
$\mathrm{B}-\mathrm{Z}$
$\mathrm{C}-\mathrm{Z}$
$\mathrm{D}-\mathrm{Z}$
9
9

7
$\mathrm{C}-\mathrm{A}$
$\mathrm{D}-\mathrm{Z}$
$\mathrm{A}-$
$\mathrm{B}-\mathrm{Z}$
5

| $\mathrm{D}-\mathrm{A}$ |
| :--- |
| $\mathrm{C}-\mathrm{Z}$ |
| B |
| $\mathrm{A}-\mathrm{Z}$ |

$A \& B$ have the most first place votes.
A gets 9 \& 5 votes (14); B gets 7 \& 3 (10)
$A$ wins the run off.

## Sequential Run off Method:

- Eliminates one choice at a time.
- Eliminate the candidate with the least first place votes.
- Those first place votes get reassigned to the person below.
- Continue until you have a winner.

A (9) - B (7) - C (5) - D (3)
$A(9)-B(7)-C(8)$
A (9) - C (15)
$C$ is the winner with a majority of votes!

## The Borda Method

- 1 st place gets $n$ points times the number of votes ranking that person first, 2nd place is $n-1$ points times the number of votes, etc.
- Sum the values together.
- Whoever has the largest sum wins.




$$
\begin{aligned}
& \mathbf{A}=4(9)+1(7)+2(5)+1(3)=56 \text { Points } \\
& \mathbf{B}=3(9)+4(7)+1(5)+2(3)=66 \text { Points } \\
& \mathbf{C}=2(9)+2(7)+4(5)+3(3)=61 \text { Points } \\
& \mathbf{D}=1(9)+3(7)+3(5)+4(3)=57 \text { Points }
\end{aligned}
$$

The winner is " $B$ " with 66 Points!

## The Condorcet Method

- The candidate that can obtain a majority over all other individual candidates.
- See how many times A beats B (is it a majority?) and A beats $C$, etc.
- If it is a majority every time, then that candidate is the winner.


| Matchup | Winner |
| :---: | :---: |
| A (9+5) vs. B (7+3) | A (14-10) |
| A (9) vs. C ( $7+5+3$ ) | C (15-9) |
| A (9) vs. D ( $7+5+3$ ) | D ( $15-9$ ) |
| B (9+7) vs. C ( $5+3$ ) | B ( $16-8$ ) |
| B ( $9+7$ ) vs. D ( $5+3$ ) | B ( $16-8$ ) |
| C (9+5) vs. D (7+3) | C (14-10) |

$B \& C$ tied; can use head to head to declare $B$ the winner.

